

UNIVERSITY OF LONDON  
B.Sc. (ENGINEERING) EXAMINATION 1964

PART III

for Internal and External Students

(21) THEORY OF STRUCTURES

Friday 15 June: 10 to 1

Answer FIVE questions only.

1. A link having a relatively small uniform section and of the shape shown in Figure 1 is under the action of a pull  $P$  applied along its longitudinal axis. The portions  $ABC$  and  $FED$  are semicircles,  $AF$  and  $CD$  are straight and parallel to each other. Draw the bending moment diagram and find the increase in the distance  $BE$  produced by the applied loads  $P$ . Consider strain energy due to bending only.

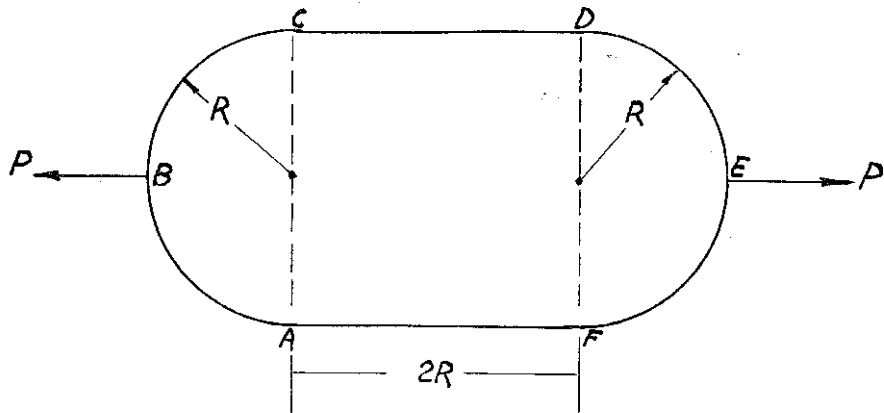


Figure 1

Turn over

2. A cantilever having a constant depth  $h$  but a varying width between A and B as shown below in Figure 2, is under the action of a vertical load  $P$  applied at point B. Find the vertical deflection of the end C.

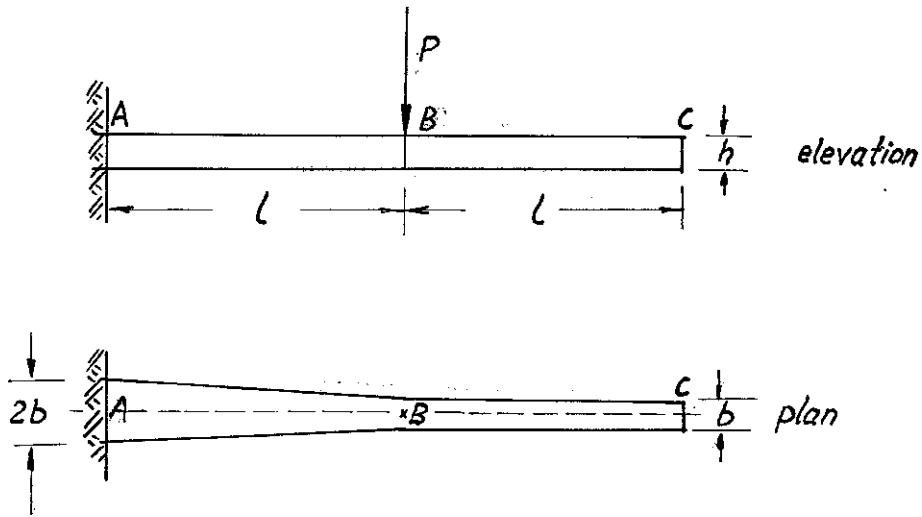


Figure 2

3. Draw the diagram of bending moments for the rigidly connected frame shown in Figure 3.

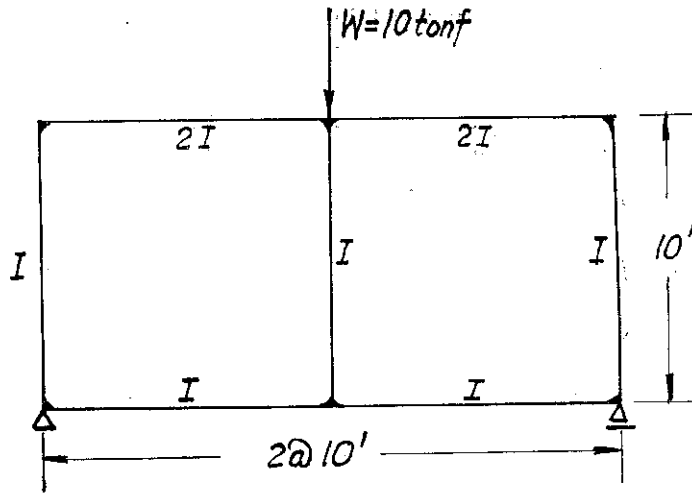


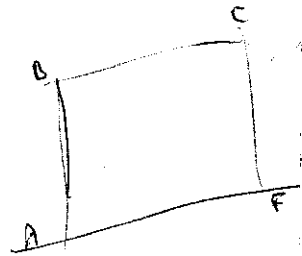
Figure 3

$$\frac{M_A}{2}$$

$$I = \frac{3b}{2} \frac{h^3}{12}$$



$$\frac{b d^3}{12}$$



4. A pin-connected space frame shown in Figure 4 consists of two regular tetrahedra  $abcd$  and  $defg$ , joined together at the common hinge  $d$  and with three flexible cables  $ag$ ,  $be$  and  $cf$ , all of equal length. The structure is pinned to the ground at the supports  $e$ ,  $f$  and  $g$  and is under the action of a horizontal load  $P$ , applied at the joint  $c$  as shown. All the members forming the tetrahedra are of the same length  $a$  and have the same cross-sectional area  $A$ . Find the forces in all members of the frame.

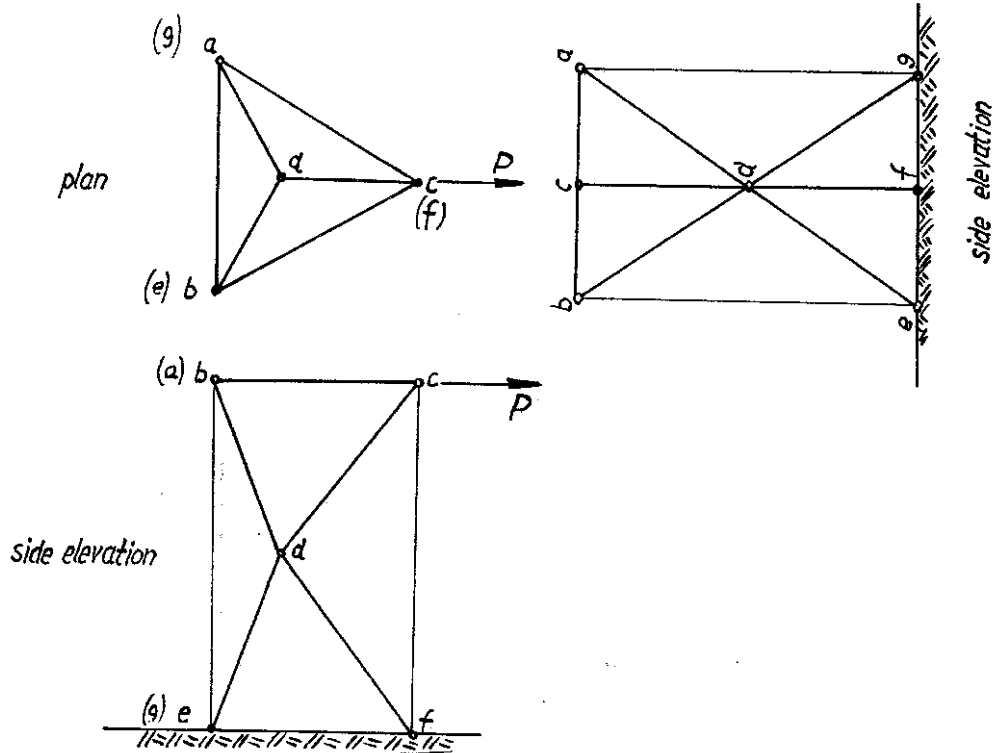


Figure 4

5. Find the shape factor for a built-up steel beam having the dimensions shown in Figure 5. The yield stress is  $15.25 \text{ tonf/in}^2$ .

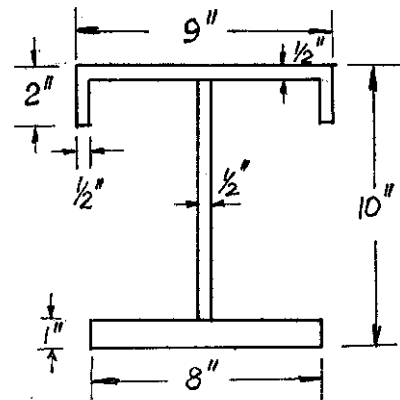


Figure 5

$$S = X Z = M$$

$$I/M = \frac{\sigma}{y}$$

$$X Z = \frac{M}{F}$$

$$Z = \frac{\sum A}{A}$$

Turn over

6. Draw the influence lines for the vertical and horizontal reaction components at  $A$ , and axial forces in members 1-2, 1-3 and 2-3 of the braced three-pinned arch shown in Figure 6. All the members are pin-connected and the external load moves along a deck connected to the panel points between  $D$  and  $E$ .

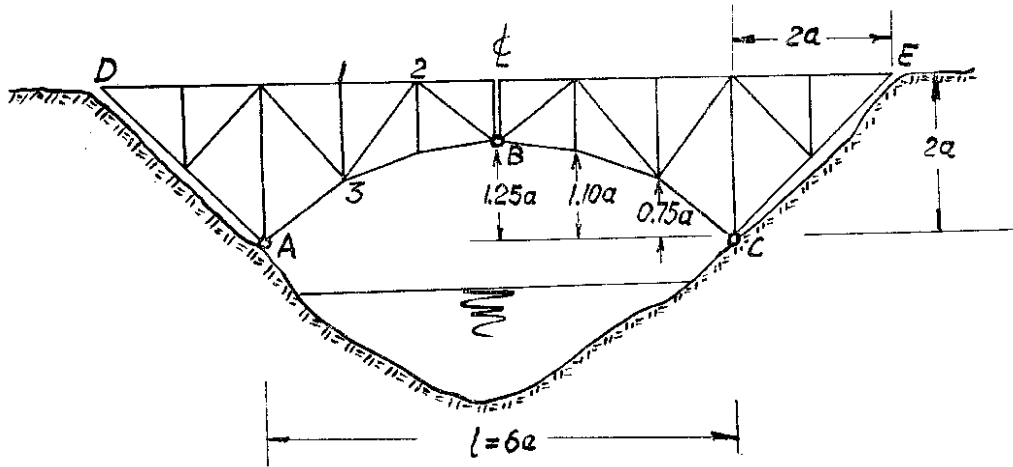


Figure 6

7. The members of the simply supported truss shown in Figure 7 are rigidly connected at all nodes. Find the expression for bending moment induced at the point of application of the vertical load  $P = 1 \text{ tonf}$ . All the members have the same cross-sectional area  $A$  and the same constant  $EI$ .

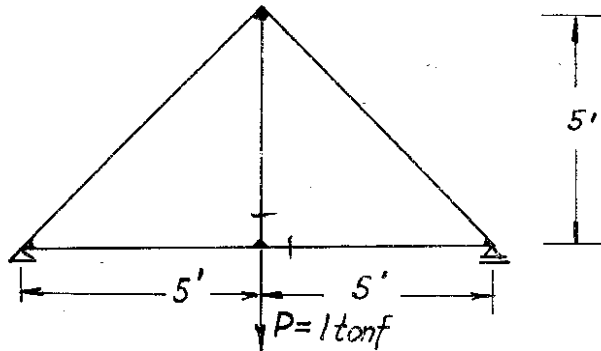


Figure 7

8. A steel tubular horizontal tie-bar carries an axial load of 1 tonf. The member is 2 ft long and is pinned at its ends. What uniformly distributed vertical load can be applied to the tie-bar to give a maximum tensile stress of  $10 \text{ tonf/in}^2$ ? The O.D. of the bar is 2 in and the wall thickness is  $1/32 \text{ in}$ . Take  $E$  as  $30 \times 10^6 \text{ lbf/in}^2$ .

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Z. S. MAKOWSKI

$2 \text{ rad} = 360$   
 $\pi = 180^\circ$   
 $1 \text{ rad} = \frac{180}{\pi}$

